

# GravCircleFormative [52 marks]

1. An object of mass  $m$  at the end of a string of length  $r$  moves in a vertical circle at a constant angular speed  $\omega$ . [1 mark]

What is the tension in the string when the object is at the bottom of the circle?

- A.  $m(\omega^2 r + g)$
- B.  $m(\omega^2 r - g)$
- C.  $mg(\omega^2 r + 1)$
- D.  $mg(\omega^2 r - 1)$

## Markscheme

A

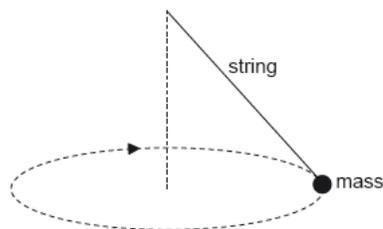
2. Newton's law of gravitation [1 mark]

- A. is equivalent to Newton's second law of motion.
- B. explains the origin of gravitation.
- C. is used to make predictions.
- D. is not valid in a vacuum.

## Markscheme

C

3. A mass at the end of a string is swung in a horizontal circle at increasing speed until the string breaks. [1 mark]



The subsequent path taken by the mass is a

- A. line along a radius of the circle.
- B. horizontal circle.
- C. curve in a horizontal plane.
- D. curve in a vertical plane.

## Markscheme

D

4. An object of mass  $m$  moves in a horizontal circle of radius  $r$  with a constant speed  $v$ . [1 mark]  
What is the rate at which work is done by the centripetal force?

A.  $\frac{mv^3}{r}$

B.  $\frac{mv^3}{2\pi r}$

C.  $\frac{mv^3}{4\pi r}$

D. zero

## Markscheme

D

A planet has radius  $R$ . At a distance  $h$  above the surface of the planet the gravitational field strength is  $g$  and the gravitational potential is  $V$ .

- 5a. State what is meant by gravitational field strength. [1 mark]

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## Markscheme

the «gravitational» force per unit mass exerted on a point/small/test mass

[1 mark]

5b. Show that  $V = -g(R + h)$ .

[2 marks]

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## Markscheme

at height  $h$  potential is  $V = -\frac{GM}{(R+h)}$

field is  $g = \frac{GM}{(R+h)^2}$

«dividing gives answer»

*Do not allow an answer that starts with  $g = -\frac{\Delta V}{\Delta r}$  and then cancels the deltas and substitutes  $R + h$*

**[2 marks]**

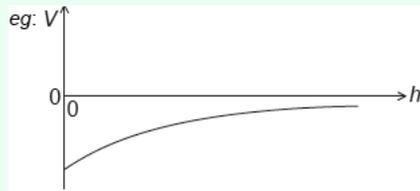
5c. Draw a graph, on the axes, to show the variation of the gravitational potential  $V$  of the planet with height  $h$  above the surface of the planet. [2 marks]



# Markscheme

correct shape and sign

non-zero negative vertical intercept



[2 marks]

- 5d. A planet has a radius of  $3.1 \times 10^6$  m. At a point P a distance  $2.4 \times 10^7$  m above the surface of the planet the gravitational field strength is  $2.2 \text{ N kg}^{-1}$ . Calculate the gravitational potential at point P, include an appropriate unit for your answer.

[1 mark]

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# Markscheme

$$V = \left\langle -2.2 \times (3.1 \times 10^6 + 2.4 \times 10^7) \right\rangle \left\langle - \right\rangle 6.0 \times 10^7 \text{ J kg}^{-1}$$

*Unit is essential*

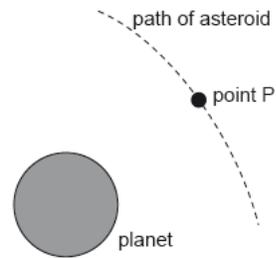
*Allow eg MJ kg<sup>-1</sup> if power of 10 is correct*

*Allow other correct SI units eg m<sup>2</sup>s<sup>-2</sup>, N m kg<sup>-1</sup>*

[1 mark]

5e. The diagram shows the path of an asteroid as it moves past the planet.

[3 marks]



When the asteroid was far away from the planet it had negligible speed. Estimate the speed of the asteroid at point P as defined in (b).

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## Markscheme

total energy at P = 0 / KE gained = GPE lost

$$\ll \frac{1}{2}mv^2 + mV = 0 \Rightarrow v = \sqrt{-2V}$$

$$v = \ll \sqrt{2 \times 6.0 \times 10^7} \Rightarrow 1.1 \times 10^4 \ll \text{ms}^{-1} \gg$$

*Award [3] for a bald correct answer*

*Ignore negative sign errors in the workings*

*Allow ECF from 6(b)*

**[3 marks]**

- 5f. The mass of the asteroid is  $6.2 \times 10^{12}$  kg. Calculate the gravitational force experienced by the **planet** when the asteroid is at point P. [2 marks]

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## Markscheme

### ALTERNATIVE 1

force on asteroid is « $6.2 \times 10^{12} \times 2.2 =$ »  $1.4 \times 10^{13}$  «N»

«by Newton's third law» this is also the force on the planet

### ALTERNATIVE 2

mass of planet =  $2.4 \times 10^{25}$  «kg» «from  $V = -\frac{GM}{(R+h)}$ »

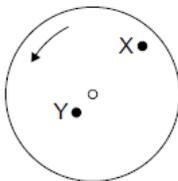
force on planet «

$$\frac{GMm}{(R+h)^2} = 1.4 \times 10^{13} \text{ «N»}$$

*MP2 must be explicit*

**[2 marks]**

6. A horizontal disc rotates uniformly at a constant angular velocity about a central axis normal to the plane of the disc. [1 mark]



Point X is a distance  $2L$  from the centre of the disc. Point Y is a distance  $L$  from the centre of the disc. Point Y has a linear speed  $v$  and a centripetal acceleration  $a$ .

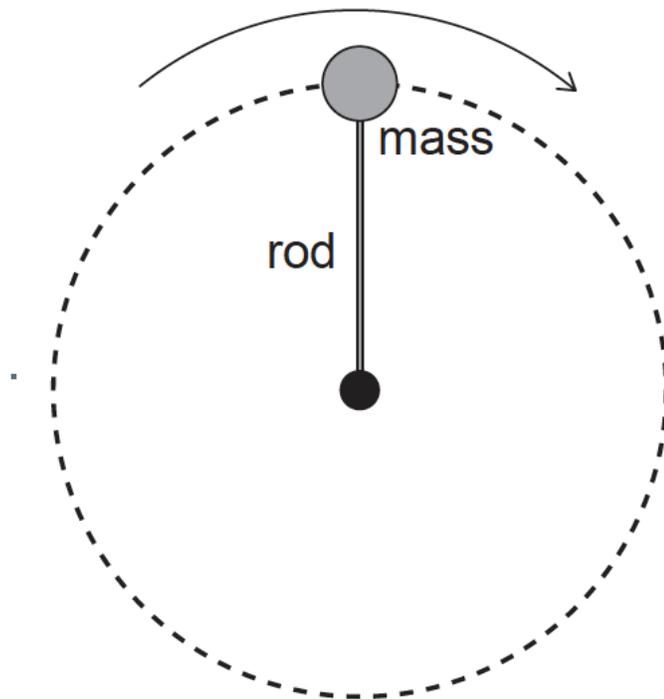
What is the linear speed and centripetal acceleration of point X?

|    | Linear speed of X | Centripetal acceleration of X |
|----|-------------------|-------------------------------|
| A. | $v$               | $a$                           |
| B. | $2v$              | $2a$                          |
| C. | $v$               | $2a$                          |
| D. | $2v$              | $4a$                          |

# Markscheme

B

7. A mass connected to one end of a rigid rod rotates at constant speed in a vertical plane [1 mark] about the other end of the rod.



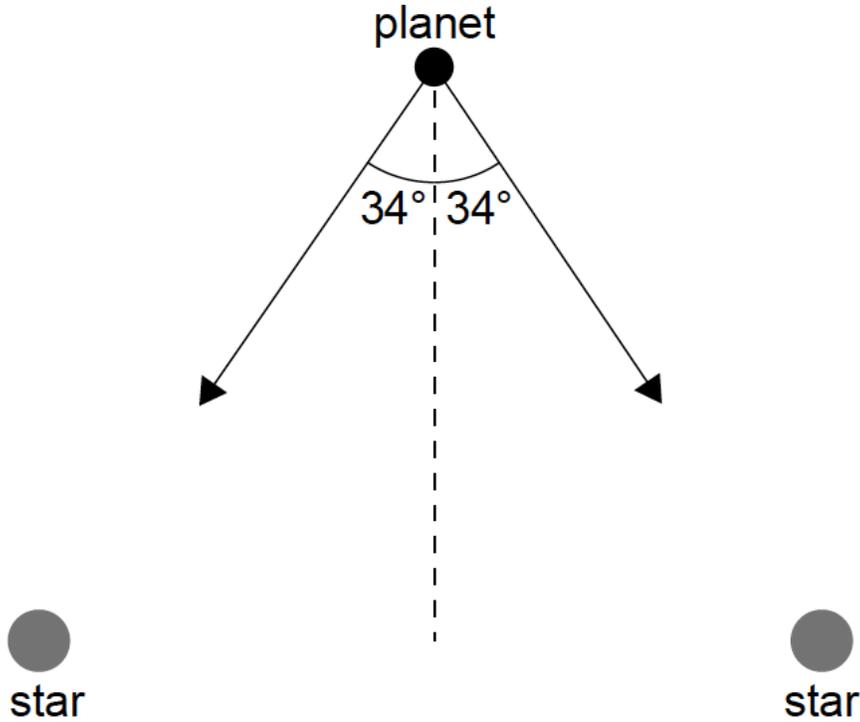
The force exerted by the rod on the mass is

- A. zero everywhere.
- B. constant in magnitude.
- C. always directed towards the centre.
- D. a minimum at the top of the circular path.

# Markscheme

D

The two arrows in the diagram show the gravitational field strength vectors at the position of a planet due to each of two stars of equal mass  $M$ .



Each star has mass  $M=2.0 \times 10^{30}$ kg. The planet is at a distance of  $6.0 \times 10^{11}$ m from each star.

- 8a. Show that the gravitational field strength at the position of the planet due to **one** of the [1 mark] stars is  $g=3.7 \times 10^{-4}$ Nkg $^{-1}$ .

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## Markscheme

$$g = \frac{GM}{r^2} = \frac{6.67 \times 10^{-11} \times 2.0 \times 10^{30}}{(6.0 \times 10^{11})^2}$$

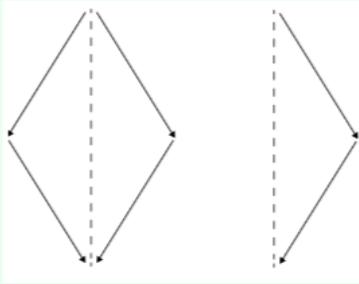
**OR**  
 $3.71 \times 10^{-4}$ Nkg $^{-1}$

- 8b. Calculate the magnitude of the resultant gravitational field strength at the position of the planet. [2 marks]

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## Markscheme

« $g_{\text{net}} = 2\cos 34^\circ$ »  $2g$  OR  $g\cos 34$  OR  $g\sin 56$  OR vector addition diagram shown



$$\llcorner g_{\text{net}} = \llcorner 2 \times 3.7 \times 10^{-4} \times \cos 34^\circ \Rightarrow 6.1 \times 10^{-4} \text{ N kg}^{-1}$$

9. A car travels in a horizontal circle at constant speed. At any instant the resultant horizontal force acting on the car is [1 mark]
- A. zero.
  - B. in the direction of travel of the car.
  - C. directed out from the centre of the circle.
  - D. directed towards the centre of the circle.

## Markscheme

D

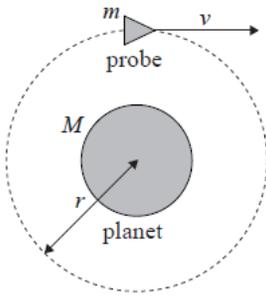
10. A spacecraft travels away from Earth in a straight line with its motors shut down. At one [1 mark] instant the speed of the spacecraft is  $5.4 \text{ km s}^{-1}$ . After a time of 600 s, the speed is  $5.1 \text{ km s}^{-1}$ . The average gravitational field strength acting on the spacecraft during this time interval is
- 1.  $5.0 \times 10^{-4} \text{ N kg}^{-1}$
  - 2.  $3.0 \times 10^{-2} \text{ N kg}^{-1}$
  - 3.  $5.0 \times 10^{-1} \text{ N kg}^{-1}$
  - 4.  $30 \text{ N kg}^{-1}$

## Markscheme

C

This question is about a probe in orbit.

A probe of mass  $m$  is in a circular orbit of radius  $r$  around a spherical planet of mass  $M$ .



(diagram not to scale)

- 11a. State why the work done by the gravitational force during one full revolution of the probe is zero. [1 mark]

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## Markscheme

because the force is always at right angles to the velocity / motion/orbit is an equipotential surface;  
*Do not accept answers based on the displacement being zero for a full revolution.*

- 11b. Deduce for the probe in orbit that its [4 marks]

(i) speed is  $v = \sqrt{\frac{GM}{r}}$ .

(ii) total energy is  $E = -\frac{GMm}{2r}$ .

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# Markscheme

- (i) equating gravitational force  $\frac{GMm}{r^2}$ ;  
to centripetal force  $\frac{mv^2}{r}$  to get result;
- (ii) kinetic energy is  $\frac{GMm}{2r}$ ;  
addition to potential energy  $-\frac{GMm}{r}$  to get result;

- 11c. It is now required to place the probe in another circular orbit further away from the planet. To do this, the probe's engines will be fired for a very short time. [2 marks]

State and explain whether the work done on the probe by the engines is positive, negative **or** zero.

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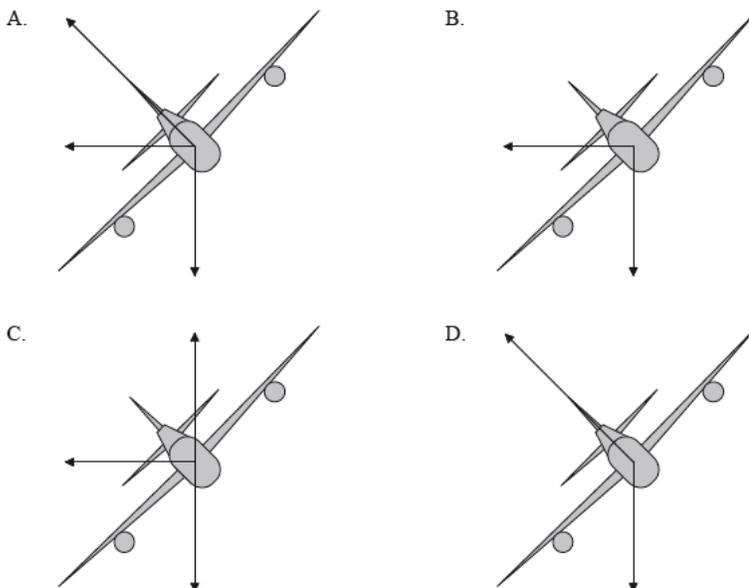
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# Markscheme

the total energy (at the new orbit) will be greater than before/is less negative;  
hence probe engines must be fired to produce force in the direction of motion /  
positive work must be done (on the probe);  
*Award [1] for mention of only potential energy increasing.*

12. An aircraft is flying at constant speed in a horizontal circle. Which of the following diagrams best illustrates the forces acting on the aircraft in the vertical plane? [1 mark]



## Markscheme

D

13. The mass of Earth is  $M_E$ , its radius is  $R_E$  and the magnitude of the gravitational field strength at the surface of Earth is  $g$ . The universal gravitational constant is  $G$ . The ratio  $\frac{g}{G}$  is equal to [1 mark]
- A.  $\frac{M_E}{R_E^2}$
  - B.  $\frac{R_E^2}{M_E}$
  - C.  $M_E R_E$
  - D. 1

## Markscheme

A

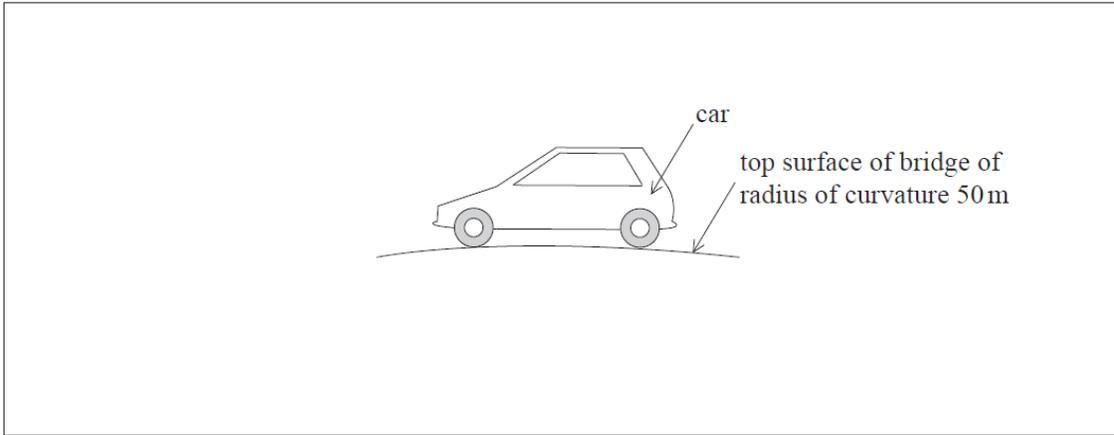
14. A communications satellite is moving at a constant speed in a circular orbit around Earth. At any given instant in time, the resultant force on the satellite is [1 mark]
- A. zero.
  - B. equal to the gravitational force on the satellite.
  - C. equal to the vector sum of the gravitational force on the satellite and the centripetal force.
  - D. equal to the force exerted by the satellite's rockets.

## Markscheme

B

This question is about circular motion.

The diagram shows a car moving at a constant speed over a curved bridge. At the position shown, the top surface of the bridge has a radius of curvature of 50 m.



15a. Explain why the car is accelerating even though it is moving with a constant speed. [2 marks]

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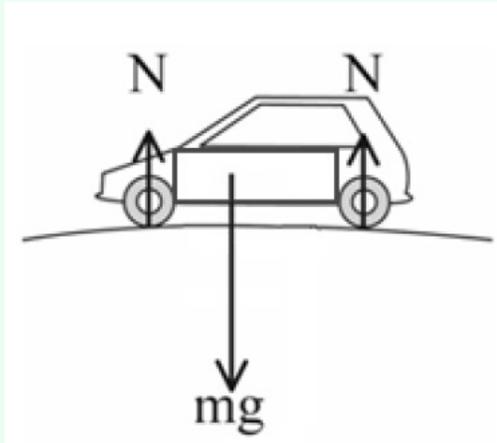
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## Markscheme

direction changing;  
velocity changing so accelerating;

15b. On the diagram, draw and label the vertical forces acting on the car in the position shown. [2 marks]

## Markscheme



weight/gravitational force/mg/w/ $F_w$ / $F_g$  and reaction/normal reaction/perpendicular contact force/ $N$ / $R$ / $F_N$ / $F_R$  both labelled; (do not allow "gravity" for "weight".)

weight between wheels (in box) from centre of mass and reactions at both wheels / single reaction acting along same line of action as the weight;

*Judge by eye. Look for reasonably vertical lines with weight force longer than (sum of) reaction(s). Extra forces (eg centripetal force) loses the second mark.*

15c. Calculate the maximum speed at which the car will stay in contact with the bridge. [3 marks]

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## Markscheme

$$g = \frac{v^2}{r};$$
$$v = \sqrt{50 \times 9.8};$$

22( $\text{ms}^{-1}$ );

Allow [3] for a bald correct answer.

This question is in **two** parts. **Part 1** is about gravitational force fields. **Part 2** is about properties of a gas.

**Part 1** Gravitational force fields

16a. State Newton's universal law of gravitation.

[2 marks]

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## Markscheme

the (attractive) force between two (point) masses is directly proportional to the product of the masses;

and inversely proportional to the square of the distance (between their centres of mass);

*Use of equation is acceptable:*

*Award [2] if all five quantities defined. Award [1] if four quantities defined.*

16b. A satellite of mass  $m$  orbits a planet of mass  $M$ . Derive the following relationship between the period of the satellite  $T$  and the radius of its orbit  $R$  (Kepler's third law).

[3 marks]

$$T^2 = \frac{4\pi^2 R^3}{GM}$$

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## Markscheme

$$G \frac{Mm}{R^2} = \frac{mv^2}{R} \text{ so } v^2 = \frac{Gm}{R};$$

$$v = \frac{2\pi R}{T};$$

$$v^2 = \frac{4\pi^2 R^2}{T^2} = \frac{Gm}{R};$$

or

$$G \frac{Mm}{R^2} = m\omega^2 R;$$

$$\omega^2 = \frac{4\pi^2}{T^2};$$

$$\frac{4\pi^2}{T^2} = \frac{GM}{R^3};$$

*Award [3] to a clear response with a missing step.*



# Markscheme

$$(i) R^3 = \frac{6.67 \times 10^{-11} \times 5.97 \times 10^{24} \times 6000^2}{4 \times \pi^2};$$

$$R = 7.13 \times 10^6 (\text{m});$$

$$h = (7.13 \times 10^6 - 6.37 \times 10^6) = 760 (\text{km});$$

Award **[3]** for an answer of 740 with  $\pi$  taken as 3.14.

$$(ii) \text{ clear use of } \Delta V = \frac{\Delta E}{m} \text{ and } V = -\frac{Gm}{r} \text{ or } \Delta E = GMm \left( \frac{1}{r_1} - \frac{1}{r_2} \right);$$

one value of potential energy calculated ( $2.37 \times 10^9$  or  $2.02 \times 10^9$ );

$$3.5 \times 10^8 (\text{J});$$

Award **[3]** for a bald correct answer.

Award **[2]** for  $7.7 \times 10^9$ . Award **[1]** for  $7.7 \times 10^{12}$ .

Award **[0]** for answers using  $mg\Delta h$ .

(iii) increased;

further from Earth / closer to infinity / smaller negative value;

Award **[0]** for a bald correct answer.